

Programming Languages

CS 214



Exam: what to expect

~60 questions

operator associativity

operator precedence

week 4 set operators: 5 questions

7 questions on history:

first Language

first implemented Implemented

Multitasking

Object Oriented Language

Procedural Language

Classes

Lists

Functional Language

Block Structue (begin and end)

Multi-Dimensional Arrays

Logic Language

Generic Types

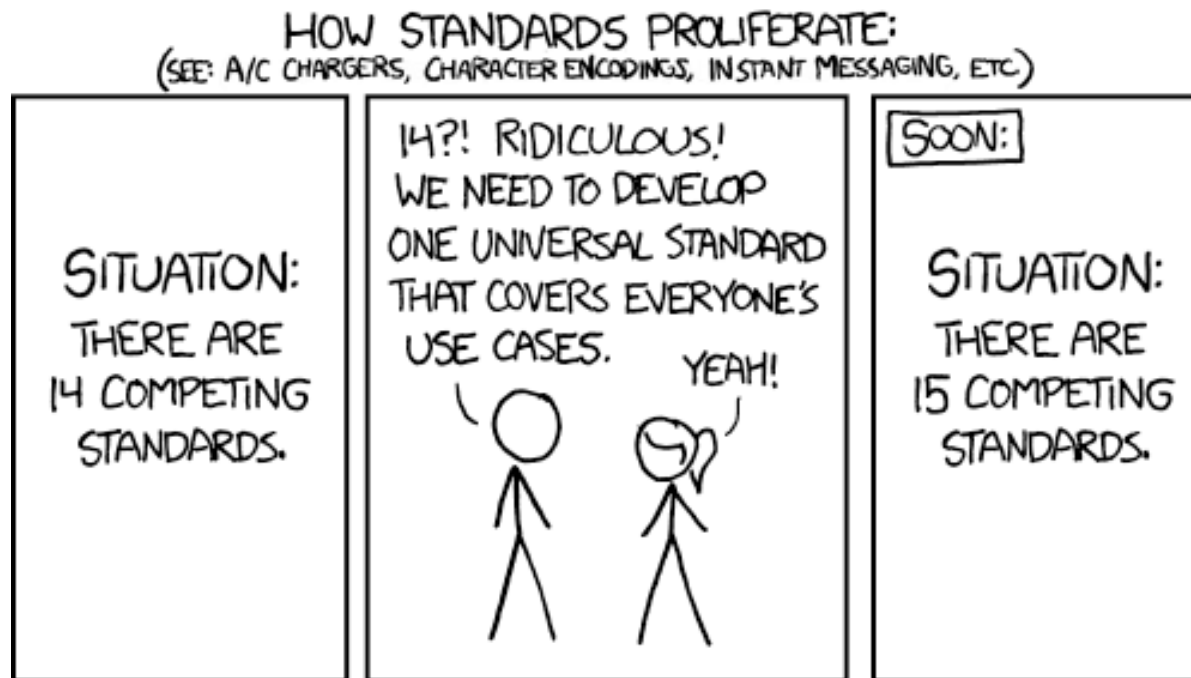
24 questions on identifying the formalisms of different implementations of branching, selection and looping.

prove ambiguity

create a bnf



“Language Independent Description”



Types

A `type` is a set V of values, and a set of operations onto V .

Examples from C++:

- The `int` type:

$$V = \{\text{INT_MIN}, \dots, -1, 0, 1, \dots, \text{INT_MAX}-1, \text{INT_MAX}\}$$
$$O = \{\ll, \gg, +, -, *, /, \%, =, ++, --, \dots\}$$

- The `char` type:

$$V = \{\text{NUL}, \dots, '0', \dots, '9', \dots, 'A', \dots, 'Z', \dots, 'a', \dots, 'z', \text{DEL}\}$$
$$O = \{\ll, \gg, =, ++, --, \text{isupper}(), \text{islower}(), \text{toupper}(), \dots\}$$

- The `string` type:

$$V = \{\text{"", "A", "B", "C", \dots, "AA", "AB", "AC", \dots, "AAA", \dots}\}$$
$$O = \{\ll, \gg, +, +=, [], \text{find}(), \text{substr}(), \dots\}$$


Fundamental Types

Let's assume the existence of some basic (primitive) types:

Name	V	C++	Ada	Smalltalk	Lisp
<i>bool</i>	false, true	<i>bool</i>	<i>boolean</i>	<i>Boolean</i>	<i>boole</i>
<i>char</i>	the set of chars	<i>char</i>	<i>character</i>	<i>Character</i>	<i>character</i>
<i>int</i>	the integers	<i>int</i>	<i>integer</i>	<i>Integer</i>	<i>integer</i>
<i>real</i>	the reals	<i>double</i>	<i>float</i>	<i>Float</i>	<i>real</i>

Such “primitive” types require little memory:

- *bool*—a single bit
- *int*—a single word
- *char*—1-2 bytes
- *real*—1-2 words



Non-Fundamental Types

New, non-fundamental types can be built from existing types:

- _____ types (arrays, vectors, lists, etc.) store multiple values of _____ type.
- _____ types (records, structs, classes, etc.) store multiple values of _____ types.

A _____ is a formal mechanism for modeling a new type that is _____, using the mathematics of _____.

A type constructor has 3 components:

- The _____ used to denote that constructor;
- The _____ that constructor; and
- The _____ associated with that constructor.



Set Constructor I: _____

Kleene Closure is a formalism for modeling _____.

- The Kleene Closure of a set A is denoted _____
- The Kleene Closure of a set is the set of all tuples that can be formed using elements of that set.

Example: The Kleene Closure of `bool` -- _____ -- is the infinite set:

`{ (), (false), (true), (false, false), (false, true), (true, false), (true, true), (false, false, false), ... }`

- For a tuple $t \in A^*$, the operations include:

<code>null(A*)</code>	<code>→ bool</code>	<code>null(())</code>	<code>→ true</code>
		<code>null((false))</code>	<code>→ false</code>
		<code>null((true))</code>	<code>→ false</code>

<code>first(A*)</code>	<code>→ A</code>	<code>first((true, false))</code>	<code>→ true</code>
		<code>first((false, true))</code>	<code>→ false</code>

<code>rest(A*)</code>	<code>→ A*</code>	<code>rest((true, true, false))</code>	<code>→ (true, false)</code>
		<code>rest((false, true, true))</code>	<code>→ (true, true)</code>



Kleene Closure Examples

If _____ is the set of ASCII characters, what is _____ ?

- The infinite set of all tuples formed from ASCII characters.
(in C, the set of all character strings).

The C/C++ notation: "Hello"
is just a different syntax for: ('H', 'e', 'l', 'l', 'o')

Thus, _____ denotes a sequence (array, list, ...) of integers;

```
int intStaticArray[32];  
int * intDynamicArray = new int[n],  
vector<int> intVec;  
list<int> intList;
```

_____ denotes a sequence (array, list, ...) of reals;
and so on.



Sequence Operations

Sequence operations can be built via *null()*, *first()*, and *rest()*

- An output operation can be defined like this (pseudocode):

```
void print(ostream& out, int * a) {
    if ( !null(a) ) {
        out << first(a) << ' ';
        print(out, rest(a));
    }
};
```

- A subscript operation can be defined like this (pseudocode):

```
char& operator[](char * a, int i){
    if (i <= 0)
        return first(a);
    else
        return operator[](rest(a), i-1);
};
```

In Lisp:

_____ is called *car*

_____ is called *cdr*.



Set Constructor II: _____

Product is a formalism for modeling _____.

– The product of two sets A and B is denoted $A \times B$.

– $A \times B$ consists of all ordered pairs (a, b) : $a \in A, b \in B$.

$A \times B \times C$ consists of all ordered triples (a, b, c) : $a \in A, b \in B, c \in C$.

$A \times B \times \dots \times N$ consists of all ordered n -tuples (a, b, \dots, n) :
 $a \in A, b \in B, \dots, n \in N$.

Example: the set $bool \times char$ has 256 elements:

$\{ \dots, (true, 'A'), (false, 'A'), (true, 'B'), (false, 'B'), \dots, \}$.

– Operations associated with product are the *projection* operations:

○ _____, applied to an n -tuple (s_1, s_2, \dots, s_n) returns s_1 .

○ _____, applied to an n -tuple (s_1, s_2, \dots, s_n) returns s_2 .

○ _____, applied to an n -tuple (s_1, s_2, \dots, s_n) returns s_n .



Product Example: C++ structs

```
struct Student
{
    int id;
    double gpa;
    char gender;
};
Student aStudent;
```

Formally, a Student consists of:

Formally, a particular Student:

```
aStudent.id = 12345;
aStudent.gpa = 3.75;
aStudent.gender = 'F';
```

is the 3-tuple: (12345, 3.75, 'F').

The C++ “dot-operator” is a projection operation:

```
cout << aStudent.id           // extract id
     << aStudent.gpa          // extract gpa
     << aStudent.gender       // extract gender
     << endl;
```



Set Constructor III: _____

Function is a formalism for *subprograms* (type operations).

- The set of all functions from a set A to a set B is denoted _____.
- A particular function f mapping A to B is denoted _____.

Examples:

- The set _____ contains all functions that map _____ values into _____ values, some C examples of which include:

`isupper('A') → true`

`islower('A') → false`

`isalpha('A') → true`

`isdigit('A') → false`

`isalnum('A') → true`

`isspace('A') → false`

- The set _____ contains all functions that map _____ values into _____ values, some C examples of which include:

`tolower('A') → 'a'`

`toupper('a') → 'A'`



Function Arity

Product serves to denote an aggregate or an argument-list.

What does this set contain? _____

- All functions that map pairs of integers to a boolean.

Examples?

$==(2, 3) \rightarrow \text{false}$

$!=(2, 3) \rightarrow \text{true}$

$<((2, 3)) \rightarrow \text{true}$

$>((2, 3)) \rightarrow \text{false}$

Definition:

The number of operands an operation requires is its _____.

- Operations with 1 operand are _____ operations, with _____.
- Operations with 2 operands are _____ operations, with _____.
- Operations with 3 operand are _____ operations, with _____.
- ...



Example Ternary Operation

The C/C++ conditional expression has the form:

producing _____ if _____ is true, and
producing _____ if _____ is false.

Here is a simple *minimum()* function using it:

```
int minimum(int first, int second) {  
    return (first < second) ? first : second;  
};
```

The C/C++ conditional expression is a _____;
the one above can be formally described by:



Example Ternary Operation: Pluralization

```
cout << "Enter the number of values you have to process: ";
int n;
cin >> n;
    ... read and process the n values
cout << "You entered " << n << "value"
    << (n == 1) ? "." : "s." // based on n, pluralize 'value'
    << endl;
```

This ternary operation is from $(\text{bool} \times \text{char}^* \times \text{char}^*) \rightarrow \text{char}^*$

Operator Positioning

Operators are also categorized by their position relative to their operands:

- _____ operators appear _____ their operands: 1 + 2
 - _____ operators appear _____ their operands: + 1 2
 - _____ operators appear _____ their operands: 1 2 +
- * + 2 3 - 4 2 ≡ (2 + 3) * (4 - 2) ≡ 2 3 + 4 2 - *

Prefix, infix, and postfix notation are different conventions for the same thing; a language may choose any of them:

<u>C++ Expr</u>	<u>Category</u>	<u>Value</u>	<u>Lisp Expr</u>	<u>Category</u>	<u>Value</u>
$x < y$	binary, infix	true, false	$(< x y)$	binary, prefix	true, false
$++x$	unary, prefix	$x+1$	$(incf x)$	unary, prefix	$x+1$
$11 + 12$	binary, infix	23	$(+ 11 12)$	binary, prefix	23
$!flag$	unary, prefix	neg. of <i>flag</i>	$(not\ flag)$	unary, prefix	neg. of <i>flag</i>
$cout \ll x$	binary, infix	cout	$(princ\ x\ str)$	binary, prefix	x
$x++$	unary, postfix	x	None		



Review

There are four fundamental types:

– *bool, char, int, real*

New types can be modeled using three set formalisms:

– _____ (sequence types): _____

Operations: _____

– _____ (aggregate types): _____

Operations: _____

– _____ (type operations): _____

These _____ provide a mechanism for



Practice Using Constructors

Give formal descriptions for:

- The *logical and* operation ($\&\&$):

- How many operands does it take?
- What types are its operands?
- What type of value does it produce?

So $\&\&$ is a member of

- The C++/*STL substring* operation ($str.substr(i,n)$):

- How many operands does it take?
- What types are its operands?
- What type of value does it produce?

So $substr()$ is a member of:

- For you: The *logical negation* operation (!):



Python's Genius

By including **self** in the list of parameters, python makes the context of the function abundantly clear

Class MyClass:

```
def __init__(self):  
    self.total = 0  
  
def add(self, a, b)  
    self.total = a + b  
    return self.total
```



Logical Negation (!)

How many operands does it have? _____

What types are they? _____

What type of value does it produce? _____

Then ! is a member of? _____

More Practice

- For you: this *C++ record*:

```
struct Student {  
    int myID;  
    string myName;  
    bool iAmFullTime;  
    double myGPA;  
};
```



C++ Student Structure

As an aggregate type,

Student is a member of:

More Practice

- For you: this *C++ record*:

```
struct Student {  
    int myID;  
    string myName;  
    bool iAmFullTime;  
    double myGPA;  
};
```

- For you: an *accessor* method:

```
struct Student {  
    int myID;  
    int getId() const;  
    string myName;  
    bool iAmFullTime;  
    double myGPA;  
};
```



C++ Accessor Method

As a method/function:

How many operands? _____

What are their types? _____

What type of value does it return? _____

Then `getID()` is a member of: _____

More Practice

- For you: this *C++ record*:

```
struct Student {  
    int myID;  
    string myName;  
    bool iAmFullTime;  
    double myGPA;  
};
```

- For you: an *accessor* method:

```
struct Student {  
    int myID;  
    int getId() const;  
    string myName;  
    bool iAmFullTime;  
    double myGPA;  
};
```

- How does this affect our *Student* description?



Adding an Accessor to Student

```
struct Student {  
    int myID;  
    int getId() const;  
    string myName;  
    bool iAmFullTime;  
    double myGPA;  
};
```

More Practice (ii)

- For you: A “complete” class:

```
class Student {
public:
    Student();
    Student(int, string, bool, double);
    int getID() const;
    string getName() const;
    bool getFullTime() const;
    double getGPA() const;
    void read(istream &);
    void print(ostream &) const;
private:
    int    myID;
    string myName;
    bool   iAmFullTime;
    double myGPA;
};
```



Class Student

```
class Student {
public:
    Student();
    Student(int, string, bool, double);
    int getID() const;
    string getName() const;
    bool getFullTime() const;
    double getGPA() const;
    void read(istream &);
    void print(ostream &) const;
private:
    int    myID;
    string myName;
    bool   iAmFullTime;
    double myGPA;
};
```

Summary

A type consists of _____ and _____.

There are four *primitive types*: _____

The set constructors:

- _____ (to represent sequences)
- _____ (to represent aggregates and function parameters)
- _____ (to represent operations)

provide a formal way to model new (non-primitive) types, independent of any particular programming language:

→ Use the _____ and _____ to represent the type's _____

→ Use the _____ constructor to represent the type's _____

